

# IONOSPHERIC ACTIVITY STUDIES IN THE TERRITORY OF LATVIA USING RINEX BASE STATION DATA

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## 1. Purpose

The purpose of this study is to develop a computer algorithm that would independently analyze and graphically display GNSS post-processing data from the LatPos network's Continuously Operating Reference Stations (CORS) in Latvia in order to obtain information about ionospheric activity.

The output of the algorithm, specifically the obtained information about ionospheric activity, will help increase work productivity and assist users when GNSS data is partially missing. It will support Global Navigation Satellite System (GNSS) Real-Time Kinematic (RTK) measurements by providing visually interpretable graphs that reflect Total Electron Content (TEC) fluctuations and their effect on the accuracy of GNSS observations [2, 4, 7, 8, 9, 10].

Provision of visually perceptible graphs that reflect Total Electron Content (TEC) fluctuations and their impact on the accuracy of GNSS measurements will help users of Global Navigation Satellite System's (GNSS) Real Time Kinematics (RTK) survey methods to increase work productivity and provide with missing information [2, 4, 7, 8, 9, 10].

## 2. Test data

The test data used in this study are RINEX (Receiver Independent Exchange) files from the LatPos GNSS reference station network. These files contain GNSS satellite signal observations, such as L1 and L2 carrier frequencies, C/A and L2C (M) code pseudorange data, as well as signal recording timestamps.

Only NAVSTAR (U.S. – Navigation System with Timing And Ranging) GPS (Global Positioning System) data obtained from this network were used in this work. The data processing, including extraction and calculation of relevant parameters, was carried out using the Python programming environment [5, 12].

## 3. Theoretical basis

TEC is the total number of electrons in the upper layers of the ionosphere (between the GNSS satellite and the receiver), which affects (most often hinders) the propagation and accuracy of GNSS signals. TEC calculations are used based on pseudorange and carrier phase differences for NAVSTAR satellites at two carriers L1 and L2 [3, 6, 9].

$$TEC = \int_{receiver}^{satellite} N \cdot ds \quad (1)$$

Each satellite transmits two carrier signals in the form of electromagnetic waves at the following carrier frequencies  $L1 = f_1 = 1575.42$  MHz with a wavelength  $\lambda_1 = 19$  cm and  $L2 = f_2 = 1227.60$  MHz with a wavelength  $\lambda_2 = 24$  cm.

#### 4. TEC Calculation from GPS Observations

Pseudodistances obtained from the code (C/A, L2C (M)) travel time [2, 4, 7].

$$P = \rho + c \cdot (dT - dt) + \Delta i_i^{iono} + \Delta^{tropo} + b_i^{P,r} + b_i^{P,s} + m_i^P + \varepsilon_i^P \quad (2)$$

Where:

$i = 1, 2$  corresponding to Pseudodistances  $P_1$  (C/A) and  $P_2$  (L2C (M))

$P$  – is the code pseudorange measurement (in distance units)

$\rho$  – is the geometrical range between satellite and receiver

$c$  – is speed of light in vacuum

$dT$  – is satellite clock offset from GPS time

$dt$  – is receiver clock offset from GPS time

$\Delta i_i^{iono} = \frac{(40.3 \cdot TEC)}{f_i^2}$  ionospheric delay

$f_i$  – is the carrier frequency  $L_i$

$\Delta^{tropo}$  – tropospheric delay

$b_i^{P,r}$  – are the receiver instrumental delays on  $P$

$b_i^{P,s}$  – are the satellite instrumental delays on  $P$

$m_i^P$  – multipath effect on  $P$

$\varepsilon_i^P$  – receiver noise on  $P$

Carrier phase observations are obtained from the carrier signal travel time [2, 4, 7, 9, 11].

$$\Phi_i = \lambda_i \cdot \phi_i = \rho + c \cdot (dT - dt) + \lambda_i + N_i - \Delta i_i^{iono} + \Delta^{tropo} + b_i^{\Phi,r} + b_i^{\Phi,s} + m_i^\Phi + \varepsilon_i^\Phi \quad (3)$$

Where:

$\Phi_i$  – are carrier phase observation (in distance units)

$\phi_i$  – are carrier phase observation (in cycles)

$\lambda = c/f$  is the wavelength

$N_i$  – are the unknown number of  $L_i$  integer carrier phase ambiguities

$b_i^{\Phi,r}$  – are the receiver instrumental delays on  $\Phi$

$b_i^{\Phi,s}$  – are the satellite instrumental delays on  $\Phi$

$m_i^\Phi$  – multipath effect on  $\Phi$

$\varepsilon_i^\Phi$  – receiver noise on  $\Phi$

This formula describes the GPS pseudorange ( $P$  and  $\Phi$ ) measurement, including various factors that affect the signal path and time measurements.

TEC is the number of free electrons per square meter along the path of an electromagnetic wave traveling between a GPS satellite and a ground-based receiver. It is an important parameter in ionospheric studies and navigation corrections.

TEC is typically measured using GPS signals by analyzing the differences in pseudorange and carrier phase measurements between the two main GPS frequencies – L1 and L2.

Subtracting pseudorange measurements for L1 and L2 frequencies:

$$P_2 - P_1 = 40.3 \cdot TEC (1/f_2^2 - 1/f_1^2) \quad (4)$$

By rearranging this expression, TEC can be expressed as:

$$TEC = \frac{(P_2 - P_1)}{40.3 \cdot (1/f_2^2 - 1/f_1^2)} \quad (5)$$

When calculating a denominator containing known numerical values:

$$40.3 \cdot (1/f_2^2 - 1/f_1^2) = 1.05046 \times 10^{-5}$$

TEC simplifies to:

$$TEC = (P_2 - P_1) \cdot 95215 \quad (6)$$

where 95215 is the scaling factor in TEC electrons/m<sup>2</sup>.

TEC can be alternatively expressed as Total Electron Content Units (TECU). TECU is TEC expressed as 10<sup>16</sup> electrons/m<sup>2</sup>.

$$TEC (TECU) = (P_2 - P_1) \cdot 9.52 \quad (7)$$

This value is widely used in scientific literature [15, 16].

GPS pseudorange and carrier phase measurements can be used to calculate TEC in the ionosphere. If TEC is expressed in electrons/m<sup>2</sup>, the factor 95215 is used, and if TEC is expressed in TECU units, the factor 9.52 is used.

TEC calculation based on pseudoranges (TEC P) and carrier phase differences (TEC Φ) is described below.

Combining the pseudorange observations  $P$ , we obtain the TEC value [2, 6, 10, 14]:

$$TEC P = 9.52 \cdot (P_2 - P_1) + \text{various errors} \quad (9)$$

In turn, combining the carrier phase observations  $\Phi_i$ , we obtain:

$$TEC \Phi = 9.52 \cdot (\Phi_1 - \Phi_2) - (N_1 \lambda_1 - N_2 \lambda_2) + \text{various errors} \quad (10)$$

Calculating the difference between these two quantities resolves the uncertainty.

$$TEC L = TEC \Phi - (TEC \Phi - TEC P) \quad (11)$$

TEC is essential in geophysics and has applications in navigation measurement corrections for single-frequency receivers, as there is no way to calculate this uncertainty.

Traditionally, TEC was measured using the Faraday rotation effect on a linearly polarized plane wave.

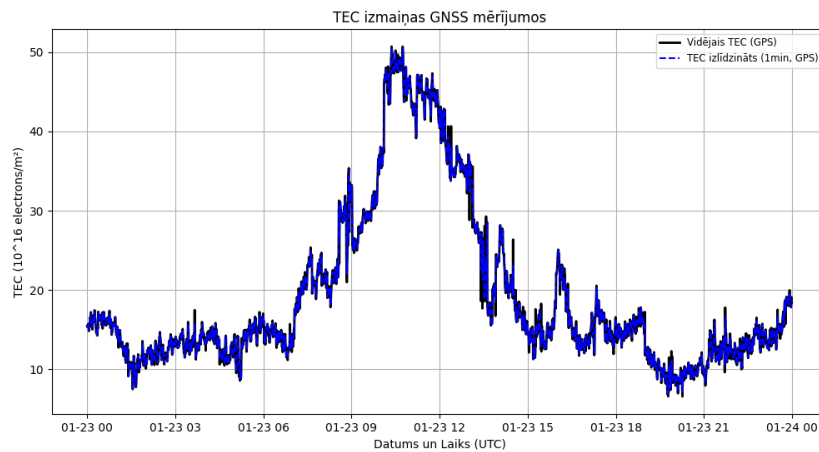
### 5. Development progress

Python Software version 3.13.1 with georinex, numpy, pandas, matplotlib, gzip and other libraries were used to automate the calculations.

In order to test the operation of the algorithm time effectively, a 10-minute RINEX file was created.

Figure 1. displays test data analysis for a 10-minute RINEX file on 23.01.2025 LGIA (Latvian Geospatial Information Agency).

### 6. Results



**Fig. 1.** Test data TEC graph of 23.01.2025

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